

Completing the Square

Write each of these expressions in the form $(x + a)^2 + b$

(a)	(b)	(c)	(d)
$x^2 + 8x + 3$ $= (x + 4)^2 - 16 + 3$ $= (x + 4)^2 - 13$	$x^2 + 6x - 1$ $= (x + 3)^2 - 9 - 1$ $= (x + 3)^2 - 10$	$x^2 - 4x + 11$ $= (x - 2)^2 - 4 + 11$ $= (x - 2)^2 + 7$	$x^2 - 10x - 5$ $= (x - 5)^2 - 25 - 5$ $= (x - 5)^2 - 30$
(e)	(f)	(g)	(h)
$x^2 - 2x + 7$ $= (x - 1)^2 - 1 + 7$ $= (x - 1)^2 + 6$	$x^2 + 4x$ $= (x + 2)^2 - 4$	$x^2 - 12x + 2$ $= (x - 6)^2 - 36 + 2$ $= (x - 6)^2 - 34$	$x^2 + 16x + 21$ $= (x + 8)^2 - 64 + 21$ $= (x + 8)^2 - 43$
(i)	(j)	(k)	(l)
$x^2 + x + 4$ $= \left(x + \frac{1}{2}\right)^2 + \frac{15}{4}$	$x^2 + 3x - 2$ $= \left(x + \frac{3}{2}\right)^2 - \frac{17}{4}$	$x^2 - x + 9$ $= \left(x - \frac{1}{2}\right)^2 + \frac{35}{4}$	$x^2 + 5x + 3$ $= \left(x + \frac{5}{2}\right)^2 - \frac{13}{4}$
(m)	(n)	(o)	(p)
$x^2 - 20x + 35$ $= (x - 10)^2 - 65$	$x^2 + 9x - 11$ $= \left(x + \frac{9}{2}\right)^2 - \frac{125}{4}$	$x^2 - 7x$ $= \left(x - \frac{7}{2}\right)^2 - \frac{49}{4}$	$x^2 - 3x - 8$ $= \left(x - \frac{3}{2}\right)^2 - \frac{41}{4}$